



Automation of NLO Calculations - Precise Predictions for LHC Processes

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Motivation



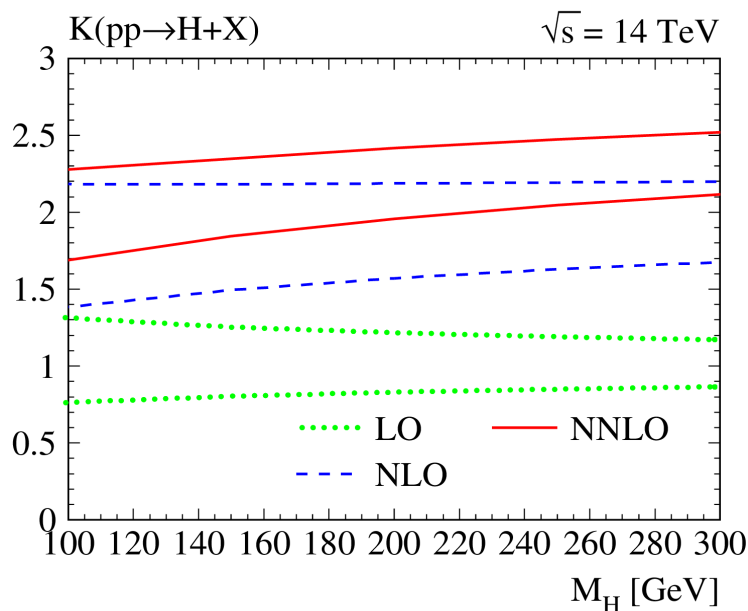
Why is this necessary / useful ?



Why is this necessary / useful ?

→ LHC relevant processes need precise predictions

Example: Higgs production:



[Harlander, Kilgore] '02

- Large corrections from higher orders
- Strong dependence on ren./fac. scale

→ LO predictions unreliable, need at least NLO

NLO calculations are hard, complicated and time consuming!



Why is this necessary / useful ?

Automation is important because

- ✓ it saves time
- ✓ avoids human mistakes
- ✓ allows to reuse building blocks
- ✓ easier to handle for the user
- ✓ not necessary to understand all details
- ✓ multipurpose



"I designed a program that allows me to run the entire plant from my computer. By the way, how's the weather back there?"

But

- ✗ For a specific task, often one can design a dedicated tool which is better suited



How can I benefit from automation ?

- It enables the user to perform complex NLO calculations.
- No need to reinvent things from scratch.
- Can be used as a black box, no need to know the internal details.
- Can also be used by experimentalists (not just a toy for theorists).
- Different tools can be combined (modular structure).



Structure of NLO



$$\sigma_{NLO} = \int_n (d\sigma^B + d\sigma^V + \int_1 d\sigma^A) + \int_{n+1} (d\sigma^R - d\sigma^A)$$

Tree level

Virtual corrections -
one loop

Real emission
(infrared divergent)

Subtraction terms: Needed to cancel infrared singularities numerically.
Idea: Add zero in suitable way to cancel infrared singularities from real emission

Several methods available:

- **Residue subtraction** [Frixione, Kunszt, Signer]
- **Dipole formalism** [Catani, Seymour],[Catani, Dittmaier, Seymour, Trocsanyi]
- **Antenna formalism** [Kosower], [Campbell,Cullen,Glover],[Gehrmann-De Ridder,Gehrmann,Glover],[Daleo,Gehrmann,Maitre],[Gehrmann-De Ridder,Ritzmann]



NLO (R)evolution



Enormous progress in recent years:

Automation of subtraction methods

- SHERPA [Gleisberg, Krauss]
- TeVJet [Seymour, Tevlin]
- MadDipole [Frederix, Gehrmann, NG]
- AutoDipole [Hasegawa, Moch, Uwer]
- HELAC-NLO [Czakon, Papadopoulos, Worek]
- MadFKS [Frederix, Frixione, Maltoni, Stelzer]

Automation of virtual corrections

- BlackHat [Berger et al.]
- Collier [Denner, Dittmaier]
- FeynArts/Formcalc/Looptools [Hahn et al.]
- GoSam [Cullen et al.]
- HELCA-NLO [Bevilacqua et al.]
- MadGolem [Goncalves Netto et al.]
- MadLoop [Hirschi et al.]
- MCFM [Campbell et al.]
- Ngluon/Njet [Badger et al.]
- OpenLoops [Cascioli et al.]
- PJFry [Fleischer et al.]
- POWHEG [Alioli et al.]
- Prospino [Beenakker et al.]
- Recola [Actis et al.]
- Rocket [Ellis et al.]
- VBFNLO [Arnold et al.]



Public package to generate subtraction terms in the Dipole formalism

- For general process in **QCD** [Frederix, Gehrmann,NG '08, '10] and **QED** [Gehrmann,NG, '10]
- Specify real emission process, e.g. $p p \rightarrow j j j$
 - Generates **Fortran** code for all necessary subtraction terms for all possible tree level processes.
 - Generates the corresponding integrated subtraction terms.
- Although MadGraph framework, completely independent and **standalone**.
 - Can be linked with other tools.

<http://madgraph.uiuc.edu>



Golem+ Samurai = GoSam

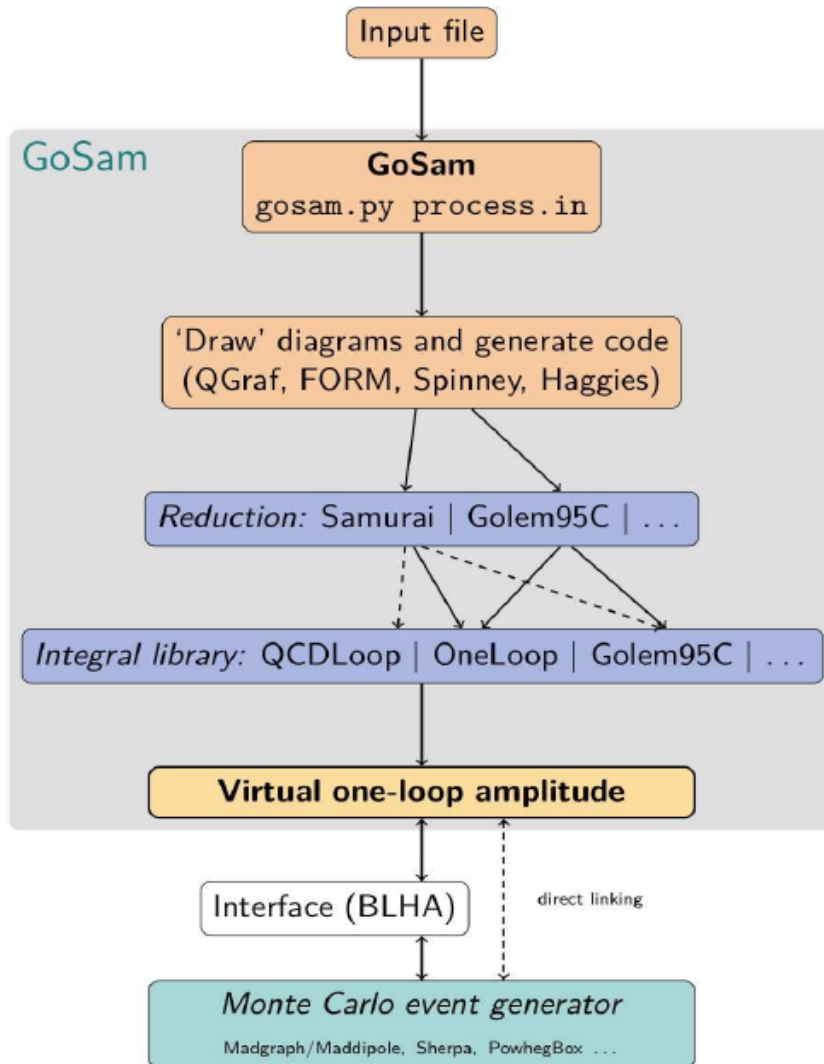
**General One Loop Evaluator of Matrix elements +
Scattering Amplitudes from Unitarity based Reduction At Integrand level
= Automated generation of virtual amplitude.**

arXiv: 1111.2034 [hep-ph] (EPJC 72, 2012)

[Cullen,NG,Heinrich,Luisoni,Mastrolia,Ossola,Reiter,Tramontano]

- Based on **Feynman diagrams**
- Generates **Fortran95** code
- Can be used for **QCD, EW, effective Higgs coupling** and **BSM**
- Interface with existing tools for real radiation and integration (MadGraph, Sherpa, Powheg)

<http://gosam.hepforge.org>



I. Input card: Specify process dependent information

II. Code generation:

- Uses QGraf [Nogueira] and
- FORM [Vermaseren]
- Writes Fortran code

III. At runtime:

Reduction of diagrams

- Integrand level (OPP) with Samurai [Mastrolia, Ossola, Reiter, Tramontano]
- Passarino-Veltman with Golem95C [Cullen et al.]
- Can be chosen at runtime
- Several integral libraries available
 - OneLoop [van Hameren]
 - QCDLoop [Ellis, Zanderighi]
 - Golem95C
- Can be linked to Monte Carlo via standardized interface (BLHA)

→ G. Luisoni T10.4



GoSam



```
ttH : bash

File Edit View Bookmarks Settings Help

greiner@pcl340b:~/GoSam/gosam-1.0/ttH> ls
codegen  diagrams-0.hh  diagrams-1.log  helicity1  helicity13  helicity4  helicity8  Makefile.conf  model.hh
common  diagrams-0.log  doc            helicity11  helicity15  helicity5  helicity9  Makefile.source
config.sh diagrams-1.hh  helicity0      helicity12  helicity3   helicity7  Makefile       matrix
```

parameters and setup
in config.f90 / model.f90

Index	1	2	3	4	5
0	-	-	0	-	-
1	+	-	0	-	-
2 → 1	-	+	0	-	-
3	+	+	0	-	-
4	-	-	0	+	-
5	+	-	0	+	-
6 → 5	-	+	0	+	-
7	+	+	0	+	-
8	-	-	0	-	+
9	+	-	0	-	+
10 → 9	-	+	0	-	+
11	+	+	0	-	+
12	-	-	0	+	+
13	+	-	0	+	+
14 → 13	-	+	0	+	+
15	+	+	0	+	+

GoSam 1.0: $gg \rightarrow Ht\bar{t}$

greiner

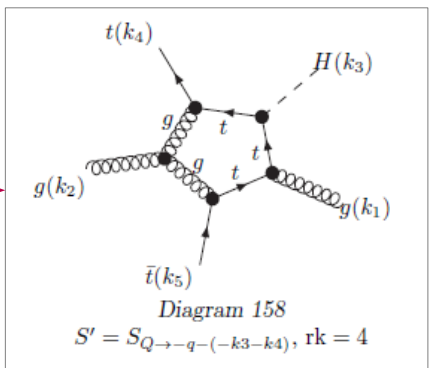
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Abstract

This process consists of 8 tree-level diagrams and 160 NLO diagrams. Golem has identified 15 groups of NLO diagrams by analyzing their one-loop integrals.

main file
matrix.f90

Detailed documentation
in process.ps





Interfacing GoSam



- **GoSam + MadDipole + MadGraph/MadEvent** [Stelzer, Long, '94], [Maltoni, Stelzer, '02]
 - NLO QCD corrections to $pp \rightarrow b\bar{b}b\bar{b}$
[Binoth, NG, Guffanti, Guillet, Reiter, Reuter '10, '11]
 - NLO QCD corrections to $pp \rightarrow W^+ W^- + 2 \text{ jets}$
including massive top loops
[NG, Heinrich, Mastrolia, Ossola, Reiter, Tramontano '12]
 - SUSY QCD corrections to neutralino pair + jet in MSSM
[Cullen, NG, Heinrich '12]
- **GoSam + Sherpa**
 - H + 2 jets in gluon fusion  H. van Deurzen, T10.6
[van Deurzen, NG, Luisoni, Mastrolia, Mirabella, Ossola, Peraro, von Soden-Fraunhofen, Tramontano '13]
 - More ready-to-go packages at <http://gosam.hepforge.org/proc>
[Luisoni, Tramontano]



Diphoton + Jet @ NLO



Diphoton + jet – Photon Fragmentation [\[Gehrmann,NG,Heinrich, '13\]](#)

- Background to $H + \text{jet}$, $H \rightarrow \gamma\gamma \rightarrow$ need NLO QCD corrections!

More than just a normal NLO calculation...



Diphoton + Jet @ NLO

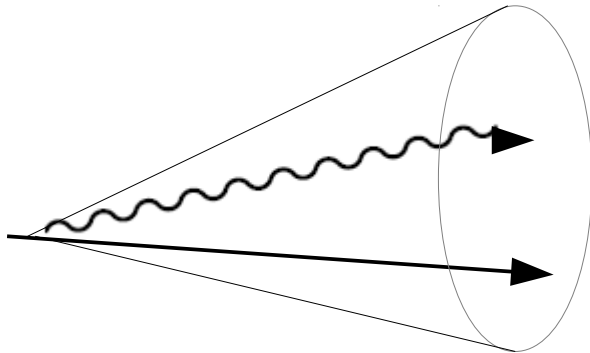


Diphoton + jet – Photon Fragmentation [\[Gehrmann,NG,Heinrich, '13\]](#)

- Background to $H + \text{jet}$, $H \rightarrow \gamma\gamma \rightarrow$ need NLO QCD corrections!

More than just a normal NLO calculation...

- Experiment: Photon accompanied by QCD stuff
- Collinear Limit between Photon and Quark resolved



Theory:

Quark and Photon collinear: **Singularity!**

- QED singularity $\rightarrow$ no cancellation with virtuals



Diphoton + Jet @ NLO



Photon Fragmentation / Cone isolation

- Photon can have two origins:
 - I. Direct radiation off quark/antiquark
 - II. Fragmentation of hadronic jets into photons
 - Non-perturbative, described by photon fragmentation function (measured)
- Collinear singularity absorbed into photon fragmentation function

→ In cone around photon

$$z = \frac{p_{T,hadr}}{p_T(p_{hadr} + p_\gamma)} \leq z_{cut}$$

- ✓ Compatible with experiment
- ✗ Theoretically complicated

Frixione Isolation criterion [Frixione '98]

- The closer to the collinear limit, the less hadronic energy is allowed.

→ Inside cone around photon with radius R_γ

$$E_{had,max}(r_\gamma) = \epsilon_\gamma p_{T,\gamma} \left(\frac{1 - \cos r_\gamma}{1 - \cos R_\gamma} \right)^{n_\gamma}$$

➡ In the limit, no hadronic energy is allowed
➡ **Finite!**

- ✓ Theoretically nice, no extra contributions needed
- ✗ Experimentally no smooth cut-off possible



Diphoton + Jet @ NLO



Status: $pp \rightarrow \gamma \gamma$: Dipbox [Binoth,Guillet,Pilon,Werlen '99] cone isolation / Frixione isolation

$pp \rightarrow \gamma j$: Jetphox [Catani et al. '02], [Aurenche et al. '06], [Belghobsi et al. '09]
cone isolation / Frixione isolation

$pp \rightarrow \gamma \gamma j$: NLOJet++ [DeDuca,Maltoni,Nagy,Trocsanyi '03] Frixione isolation

New: Comparison between the two methods

Setup: Virtuals with GoSam

Tree level /real radiation with MadGraph

Subtraction terms for QCD with MadDipole

Phase space integration with MadEvent



“normal” QCD

Additional subtraction terms for QED singularities with MadDipole

Include LO fragmentation from BFGW set.

Modular structure of automated building blocks allows easy combination.



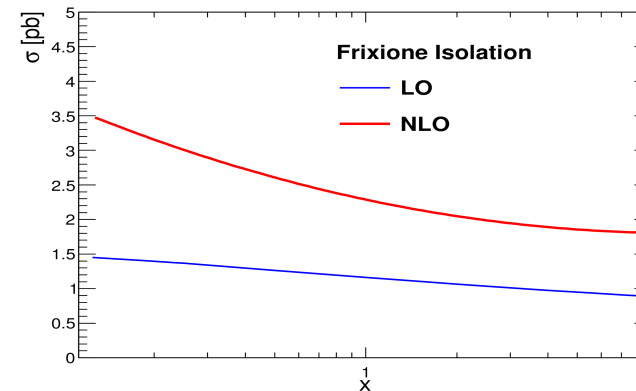
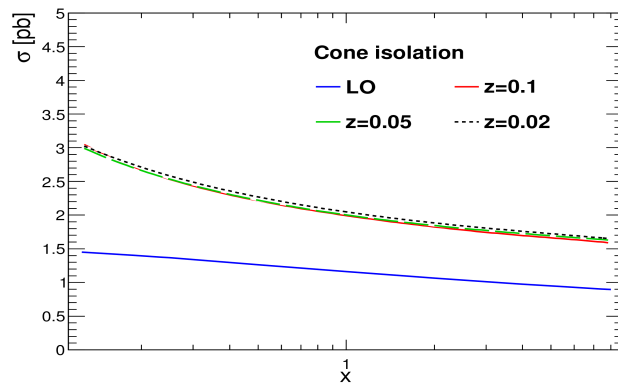
Diphoton + Jet @ NLO



Scale variation: $\mu_0^2 = \frac{1}{4} (m_{\gamma\gamma}^2 + \sum_j p_{T,j}^2)$ $\mu_r = \mu_f = \mu_F$ $\sqrt{s} = 8 \text{ TeV}$

$p_T^{\text{jet}} > 40 \text{ GeV}$, $p_T^\gamma > 20$, $|\eta^\gamma, \eta^j| \leq 2.5$, $R \geq 0.4$ $100 \text{ GeV} \leq m_{\gamma\gamma} \leq 140 \text{ GeV}$.

Inclusive cuts:



$\epsilon = 0.5$, $n = 1$

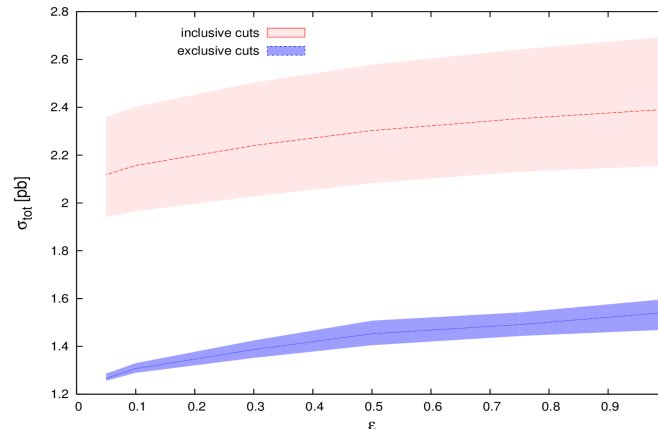
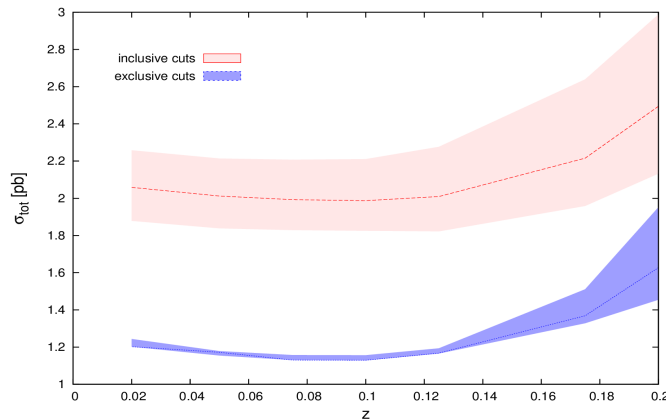
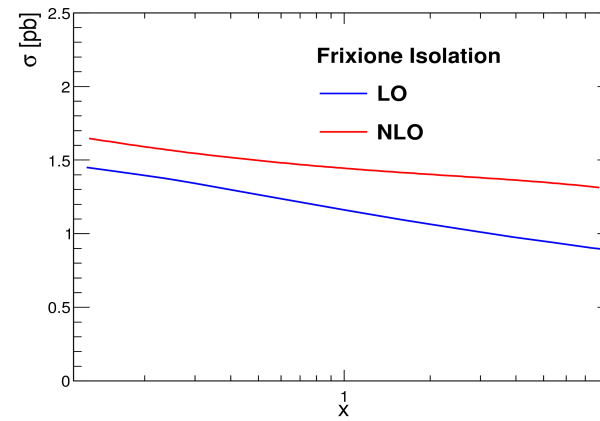
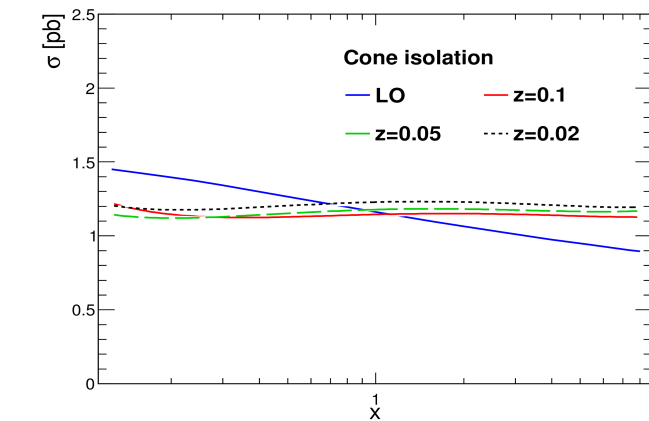
- Large K-factor ~ 2
- No reduction of scale uncertainty



Diphoton + Jet @ NLO



Impose veto on second jet (exclusive cuts): $p_{T,j2} \leq 30 \text{ GeV}$



- Reduction of scale uncertainty compared to LO.
- Strong reduction of K-factor compared to inclusive cuts.
- Cone isolation more stable under scale variation



Summary and Outlook



- Automation of NLO calculations important step for LHC processes.
- Still ongoing process, lots of room for improvements.
- Diversity of excellent tools for various purposes.
- **MadDipole:** Public standalone tool for subtraction terms in QCD and QED using dipole formalism.
- **GoSam:** Public tool for calculating virtual corrections in SM and BSM.
- **Example:** QCD corrections to Diphoton + jet including fragmentation effects.
 - Comparison between Frixione isolation and cone isolation
 - Large corrections, rescaling with global K-factor imprecise
 - Reduction of scale uncertainty requires jet veto
 - **Outlook:** Fully automated package will be made public!



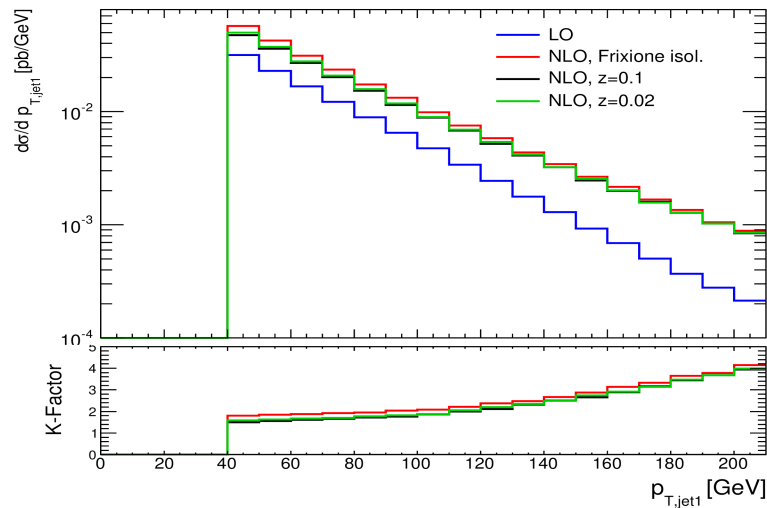
Backup slides



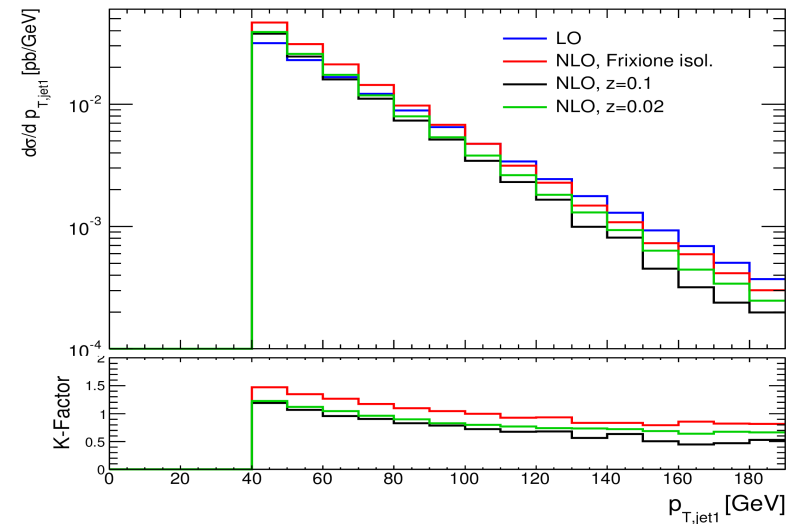
Diphoton + Jet @ NLO



In general no constant K-factors:



inclusive



exclusive

- Rescaling with global K-factor not sufficient.
- Differential K-factor sensitive on cuts.
- Counterexample: invariant mass distribution of photons

